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Mathematical model for preoperative identification of obstructed nasal subsites

Modello matematico per l’identificazione preoperatoria dei sotto-siti nasali sede di ostruzione

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SUMMARY

The planning of experimental studies for evaluation of nasal airflow is particularly challenging given the difficulty in obtaining objective measurements in vivo. Although standard rhinomanometry and acoustic rhinometry are the most widely used diagnostic tools for evaluation of nasal airflow, they provide only a global measurement of nasal dynamics, without temporal or spatial details. Furthermore, the numerical simulation of nasal airflow as computational fluid dynamics technology is not validated. Unfortunately, to date, there are no available diagnostic tools to objectively evaluate the geometry of the nasal cavities and to measure nasal resistance and the degree of nasal obstruction, which is of utmost importance for surgical planning. To overcome these limitations, we developed a mathematical model based on Bernoulli’s equation, which allows clinicians to obtain, with the use of a particular direct digital manometry, pressure measurements over time to identify which nasal subsite is obstructed. To the best of our knowledge, this is the first study to identify two limiting curves, one below and one above an average representative curve, describing the time dependence of the gauge pressure inside a single nostril. These upper and lower curves enclosed an area into which the airflow pattern of healthy individuals falls. In our opinion, this model may be useful to study each nasal subsite and to objectively evaluate the geometry and resistances of the nasal cavities, particularly in preoperative planning and follow-up.

KEY WORDS: Nose • Manometry • Fluid dynamics • Airflow • Rhinomanometry

RIASSUNTO

La realizzazione di studi sperimentali per la valutazione dei flussi aerei nasali è particolarmente indaginosa, data la difficoltà di ottenere in vivo un’accurata misurazione degli stessi. Inoltre, sebbene la rinomanometria standard e la rinometria acustica rappresentino i metodi più utilizzati nella pratica clinica, esse forniscono solo una misura globale ed approssimativa dei flussi aerei nasali, senza definirne i particolari temporali o spaziali. Allo stesso modo gli studi sulla fluidodinamica computazionale rappresentano solo una simulazione numerica, ben lontana da quelle che sono le variabili anatomiche e fisiologiche delle cavità nasali. Pertanto, ad oggi, non esistono ancora strumenti diagnosticici in grado di misurare oggettivamente la geometria delle cavità nasali, le resistenze ed il grado di ostruzione nei diversi sotto-siti nasali, elemento quest’ultimo fondamentale per una corretta programmazione chirurgica. Allo scopo di superare i limiti della diagnosi standard abbiamo elaborato un modello matematico basato sull’equazione di Bernoulli applicata alle cavità nasali di soggetti sani per lo studio dei gradienti pressori di vari sotto-siti nasali, che sono stati misurati grazie ad un particolare manometro digitale. Il nostro studio, unico in letteratura, ha identificato due curve limite che racchiudono un’area rappresentativa entro cui cadono i livelli “normali” di flusso in corrispondenza del vestibolo nasale. Il modello descritto potrebbe essere utile per studiare tutti i sotto-siti nasali sede di ostruzione ai fini di una corretta programmazione chirurgica e di un valido follow-up postoperatorio.

PAROLE CHIAVE: Naso • Manometria • Fluidodinamica • Flusso aereo • Rinomanometria
Nasal obstruction is the most common symptom observed in rhinological practice, afflicting millions of people and accounting annually for over $5.8 billion in healthcare costs in the USA alone.

Deviated nasal septum is one of the most common causes of nasal obstruction and septoplasty is the third most common surgery performed by otorhinolaryngologists. However, septal deviation may not always be the only cause of nasal obstruction. Indeed, there are many asymptomatic individuals with nasal deviation and many others suffering from nasal obstruction without septal deviation. Thus, despite successful surgical correction, many patients are not satisfied with the outcomes after septoplasty or nasal surgery in general, which might lead to medico-legal issues. Moreover, some investigators have criticised the high number of unnecessary nasal surgical procedures performed each year.

This happens because very often there are other causes responsible for nasal obstruction, such as nasal valve collapse or lateral wall insufficiency, which may alter the physiological dynamics of the nasal airflow.

For instance, in humans the physiological functions of nasal breathing (conditioning, warming and humidifying of inhaled air, smelling, etc.) are closely related to the mechanical properties of fluids. In healthy adults, most of the airflow occurs in the middle meatus, the nasal respiratory rate at rest is about 16 breaths/min and the airflow volume in a single inspiration is about 500 ml. The airflow velocity (V) depends on the strength of breath and on the width of a given nasal subsite, so that during a steady inspiration in standard conditions V is about 2-3 m/sec at the nostril level and 12-18 m/sec at the nasal valve area level.

Since the nasal valve and vestibular airflow accounts for 52.6%-78.3% of total nasal airway resistance, these sections are considered the main nasal airflow limiting structures. Thus, this anatomical and physiological narrowing at the “entrance” of the functional segment of the nose causes a significant increase in the velocity of the airflow and represents the accelerator of the inspired air. Therefore, any obstruction at this level results in a significant reduction in nasal airflow.

To summarise, effective nasal breathing requires certain airflow volumes, a pressure drop, temperature variations and the right proportions between laminar flow and turbulent flow regions, in addition to the ability to provide sufficient air to the lungs.

Hence, from a purely anatomical point of view, changes in the architecture of nasal cavities for pathological disorders, trauma or surgery may alter the nasal resistances and functions and, consequently, the mechanical properties of nasal airflow, which are strongly affected by the geometry of the airflow passage.

Unfortunately, to date, there are no diagnostic tools to objectively evaluate the geometry and mechanical properties of the nasal cavities and to measure nasal resistance and degree of nasal obstruction. Indeed, despite recent advances in the research of nasal diagnostic strategies, the currently available diagnostic tools for the study of nasal airflow and resistance have some limitations and the individual subjective sensations of the patients do not always match objective measurements.

For instance, the most widely used methods to evaluate the nasal airflow, standard rhinomanometry (RNM) and acoustic rhinometry (AR), can evaluate changes in overall nasal airflow and resistance, and measure cross-sectional areas in nasal cavity. However, due to the structural and physiological complexity of human nose, these techniques are not able to show sufficient details of dynamic airflow through the nasal cavity to fully evaluate many intranasal conditions and anatomical variations, whereas 4-phase rhinomanometry (4PR) might provide supplementary information; nonetheless, all open technical and mathematical inconsistencies conjoint with this technique have been clarified.

Furthermore, the numerical simulation of nasal airflow as computational fluid dynamics (CFD) technology, whose data are not yet validated, requires such a burden of time and resources that it cannot be routinely used.

For all these reasons, the treatment of nasal obstruction in daily clinical practice of otorhinolaryngologists represents a challenge for researchers in constantly searching for reliable objective tests to quantify nasal obstruction. To overcome these limitations and to objectively measure nasal resistances, the degree and, primarily, the subsite of nasal obstruction, we developed a mathematical model based on Bernoulli’s equation applied to clinical practice with the help of the digital DDM-MG1 manometer Endoflower (Gamerra patented, 2007).

Materials and methods

The study was performed in accordance with the principles of the 1983 Declaration of Helsinki and was approved by the local board of medical ethics. Written informed consent was obtained from all participants prior to the inclusion in the study. Forty Caucasian subjects, non-smokers suffering from cephalea and without lung disease or nasal obstruction, underwent nasal endoscopy and computed tomography (CT) scan, previously planned for the cephalea, to exclude anatomic variants or sinonasal diseases. The sample was homogeneous for age, sex and body weight (20 M 20 F; mean age 42.64 ±13.1; BMI 22.9 ±2.1 kg/m²).

To carry out pressure measurements, we used a DDM-MG1 manometer (Gamerra patented, 2007). Technical characteristics of the digital manometer were as follows: “Auto Zero” adjustable with respect of the atmospheric
pressure; range of measurement = 0 +/- 100 mbar; overrange pressure: max 300 mbar; resolution: 0.1 mbar (between 0 and 70 mbar), 0.2 mbar (between 70 and 100 mbar); accuracy at 23°C: +/- 0.5% mbar (between 0 and 70 mbar); +/- 1% mbar (between 70 and 100 mbar); temperature range: 0° to + 40°C; not condensing humidity: 10 to 90% relative humidity.

Under endoscopic guidance we placed the probe of the manometer in the nasal vestibulum corresponding to the CT imaging of the same subsite. Furthermore, to confirm the exact correspondence between the nasal point and the CT scan we chose a point easily detectable corresponding to the dome, part of the vestibulum.

Subjects were asked to slowly and deeply breathe through the nose for 4 seconds, while the nasal section was checked by video-endoscopy for the entire duration of the examination. The manometer was connected to a computer with software for visualisation and recording of pressure values. Images were acquired with an 8-slice CT scanner (LightSpeed, GE Medical Systems, Milwaukuee). The volume datasets were processed by a workstation equipped with OsiriX MD software (release 7.0.3, Pixmeo sarl, Bernex, Switzerland) and axial images were reconstructed in coronal and sagittal planes using the MPR (Multi Planar Reconstruction) protocol integrated in the software. The perimeter of air sections was outlined with “pencil” function to obtain the geometric area measurement in cm².

To estimate the airflow rate through a defined nasal section, we developed software depending on the mathematical model, based on an integral equation, concerning the minimum and maximum value of the area delimited by the two curves in figure 1 (Fig. 1), carrying out the volume of the nasal inhaled air for each inhalation.

Assuming the validity of Bernoulli’s equation, we can calculate the gauge pressure in the vestibulum by considering one central point N within this duct. In this expression, we denote the pressure in N as \( p_N \). By considering a second point O at the entrance of the nasal valve and by taking the pressure in O equal to the atmospheric pressure \( p_a \), we can write:

\[
P_N + \frac{1}{2} \rho V_N^2 = p_a \quad (1)
\]

where \( r \) is the density of air and \( V_N \) is the flow velocity in the central part of one section of the nostril, assumed to have circular shape with area \( S_N \) for simplicity. By taking a parabolic profile as the one shown in figure 2 (Figure 2), we can write:

\[
V(r, t) = V_N(t) \left[ 1 - \left( \frac{r}{R} \right)^2 \right] \quad (2)
\]

where \( r \) is radial distance from point N, \( t \) is the time measured from the beginning of inhalation, and \( R \) is the radius of the circular section of area \( S_N \) (Fig. 2).

Notice that in Eq. (1) the velocity profile \( V(r, t) \) is taken to depend on time through the time dependence of the velocity \( V_N \). Let us now calculate the flow rate through \( S_N \), so that we write:

\[
q(t) = \int_{S_N} V(r, t) dS \quad (3)
\]

where \( dS = 2\pi r dr \) is the area of an elementary ring of radius \( r \) and thickness within \( S_N \). By performing the integral, we found:

\[
q(t) = \frac{S_N}{2} V_N(t) \quad (4)
\]
The $K_1 = \int_0^T q(t) \, dt = \frac{S_n}{2} \int_0^T V_n(t) \, dt$ equation is based on the fluid dynamic criterion that the nasal airflow is concentrated in the centre of a hypothetical circumference, because most of the energy pushing the air through the nasal cavity is dissipated for effect of the laminar boundary layer flow (LBLF) against the nasal wall for which it is ineffective (Fig. 2).

Results

No complications were found during nasal manometry. In Table I we report the values of nasal sections expressed in mm$^2$, pressure in mbar and time in sec. We gathered experimental data for a deep breath of a standard-group subject. Observed data were pressure versus ($\ell$) time. The data showed that the effective velocity regarding the

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Pat = patient; sect. = section of the nose, mm$^2$; mbar. = millibar; $\ell$/s. = time/second.
The nasal airflow rate

Unlike RNM or AR, CFD shows the airflow characteristics of fluids in a computer model 17. For instance, many statistics in 3D can make accurate predictions about the variations pertaining to the need for surgical treatment implies a significant degree of subjective judgement by the surgeon 13. Nasal surgery aims at improving nasal breathing, yet decisions without temporal or spatial details. Furthermore, these methods do not suffice to reliably guide the surgeon in the choice of the best therapeutic strategy 14. In addition, they do not provide information about local details of nasal airflow, often of utmost importance from a clinical standpoint. Although AR 10 produces a more detailed evaluation of the geometry of the nasal cavities, it does not evaluate the flow field, but only the geometric boundaries. Indeed, previous studies 15 showed the validity of AR in the evaluation of functional outcomes following endoscopic surgery in correlation with volumetric CT, but it did not provide any information on the physiology of nasal pressures 16.

Unlike RNM or AR, CFD showing the airflow characteristics in 3D can make accurate predictions about the variables of fluids in a computer model 17. For instance, many authors made airflow calculations by reconstructing the nasal geometry from CT sequences of healthy subjects, whose nose was assumed to be normal in terms of flow and symmetry 18. However, they pointed out some challenging aspects related to the geometric complexity of nasal airways: the non-uniqueness of standard measurement of engineering type procedures applied to humans, the presence of physical phenomena implicated (viscosity, flow conditions, Reynolds number, wall roughness, heat transfer, humidity, fluid tissue interaction, turbulence) and, most important, the fact that CFD studies are only simulations and the predicted results derived from complex calculations of the Navier-Stokes equation, which may not represent real-life conditions 10 18.

In our study, we evaluated the nasal airflow by means of a mathematical model based on the validity of Bernoulli’s equation in the central part of the nostril. To take account of nasal airflow viscosity, we applied a quadratic velocity profile in the nostril, whose section was assumed to be circular for simplicity. Under these assumptions experimental data, reporting the gauge pressure $\Delta p(t)$ inside the nostril as a function of time, were gathered by DDM-MG, Endoflower that allowed to study the pressure inside the nose, pointing the probe in the specific nasal subsite we wanted to investigate 19 20.

The inner nasal structures were assimilated to a sequence of tubes under stationary conditions in which single particles close to the centre of the flow described laminar trajectories without energy loss 21. Although this model represents a valid approximation for airflow away from the ducts, a viscous effect could be considered in the proximity of the walls of the nasal cavity. Therefore, in our model we assumed the validity of Bernoulli’s equation in the central part of the duct, where the gradient of the velocity profile could be considered to be negligible. To achieve mathematical computed values of the volume of air during a single inhalation act, obtained pressure values were processed with data from the corresponding CT scan slide. We found that the average inhaled air volume in a single nostril in a standard-group subject during a deep breath was 221 ml, with an overall volume of 442 ml. Conversely, the literature reports values of 250 ml and 500 ml, respectively 18.

Our study, for the first time, identified two limiting curves, one below and one above an average representative curve, describing the time dependence of the gauge pressure inside a single nostril. These upper and lower curves enclosed an area into which the airflow pattern of healthy people falls. Two limiting values of the volume of inhaled

\[
\left[ t_1 \right]=0.20, s(t_2)=0.34, s(t_3)=0.43, s(t_4)=0.36, s(t_5)=0.14.\]

These statistical parameters suggested the presence of two limiting curves, one below and one above the average representative curve depicted in figure 1 (Fig. 1), enclosing an area into which the respiratory pattern of healthy people falls. Therefore, two limiting values of the volume of inhaled air per nostril exist: $K_{sup}=191$ ml and $K_{inf}=267$ ml.

Discussion

In figure 3 we show the average of the standard group measurements as full circles. By integrating this curve as a function of time we found that the volume of inhaled air in one nostril ($K_f$) was 221 ml and the total volume ($K_j$) was 442 ml.

We compared the volume of inhaled air by the standard-group subject with an average reference value (250 ml) for each nostril, as reported in the literature 7. The standard deviations (SD) for each set of data at a fixed time were then calculated:

\[
\left[ t_2 \right]=\frac{221}{250}, s(t_3)=\frac{221}{267}.
\]

Fig. 3. Fitting experimental data of gauge pressure in the nasal valve by means of the continuous function $\Delta p(t) = A t \exp(- B t^3)$ with $A=3.3914$ and $B = 0.65951$, we depicted an area into which the air respiration patterns of healthy people fall.
air per nostril, $K_{o_{\text{p}}}=191 \text{ ml}$ and $K_{o_{\text{p}}}=267 \text{ ml}$, were found. It can be argued that in order to measure nasal airflow a CT scan is needed and this would limit the clinical usefulness of the model. However, CT is not strictly necessary as the probe is placed under endoscopic guidance, which allows the perfect positioning of the probe at the chosen subsite. It is also to be considered that CT is often performed in any case as a diagnostic and preoperative tool for surgical planning.

Conclusions

In conclusion, despite recent advances in nasal diagnostics, there are still open questions on the management of nasal obstruction and on the opportunity to perform nasal surgery. Furthermore, given the lack of reliable tools to objectively measure nasal resistances and to identify the right subsite of nasal obstruction, the goal of this study was to allow clinicians to obtain pressure measurements over time at various subsites of nasal airway to identify which one are obstructed. In the present study, a mathematical model has been applied to healthy subjects to assess the normal range of resistances, with the aim to compare, in future studies, these data with those from subjects with nasal obstruction at different subsites.

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References


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