





Physical mechanisms of chromatin spatial organization

Andrea M. Chiariello¹, Simona Bianco¹, Andrea Esposito¹, Luca Fiorillo¹, Mattia Conte¹, Ehsan Irani², Francesco Musella¹, Alex Abraham¹, Antonella Prisco³ and Mario Nicodemi^{1,2,4} ib

1 Dipartimento di Fisica, Università di Napoli Federico II, and INFN Napoli, Complesso Universitario di Monte Sant'Angelo, Naples, Italy

2 Berlin Institute for Medical Systems Biology, Max-Delbrück Centre (MDC) for Molecular Medicine, Berlin, Germany

3 CNR-IGB, Naples, Italy

4 Berlin Institute of Health (BIH), MDC-Berlin, Germany

Keywords

active motors; chromatin architecture; computer simulations; machine learning; phase separation; polymer physics

Correspondence

M. Nicodemi, Dipartimento di Fisica, Università di Napoli *Federico II*, and INFN Napoli, Complesso Universitario di Monte Sant'Angelo, 80126 Naples, Italy. Email: mario.nicodemi@na.infn.it

Andrea M. Chiariello and Simona Bianco equally contributing authors

(Received 25 September 2020, revised 22 January 2021, accepted 11 February 2021)

doi:10.1111/febs.15762

conformation in the cell nucleus serving vital functional purposes, yet their folding principles remain poorly understood at the single-molecule level. Here, we summarize recent approaches from polymer physics to comprehend the physical mechanisms underlying chromatin architecture. In particular, we focus on two models that have been supported by recent, growing experimental evidence, the Loop Extrusion model and the Strings&Binders phase separation model. We discuss their key ingredients, how they compare to experimental data and some insight they provide on chromatin architecture and gene regulation. Progresses in that research field are opening the possibility to predict how genomic mutations alter the network of contacts between genes and their regulators and how that is linked to genetic diseases, such as congenital disorders and cancer.

In higher eukaryotes, chromosomes have a complex three-dimensional (3D)

Introduction

New high-throughput technologies based on sequencing, such as Hi-C, and super-resolution microscopy [1,2] are providing detailed, quantitative information about the architecture of the genome and, in particular, on the network of interactions formed by regulatory regions and their target genes [3–5]. Strong contact loops are found genome-wide between single pairs of distal DNA sites such as genes and enhancers [6]. Chromatin is also structured into a sequence of megabase sized regions, named Topological Associating Domains (TADs) [7,8], marked by strong self-interactions, which are thought, e.g., to confine the activity of enhancers to their proper targets while TAD boundaries act as spatially insulating structures. A/B compartments have also been discovered, i.e., domains of active and repressed chromatin having a size in the range of tens of Mbs [9]. Additionally, complex architectural patterns exist both at the sub-TAD level [10] and at larger scales, as TADs form higher-order structures (meta-TADs) [11] arranged in a hierarchy of domains-within-domains across genomic scales up to encompassing A/B compartments and entire chromosomes. The organization of the genome inside the nucleus typically involves multiple contacts, e.g., triplets, between distal regions such

Abbreviations

CTCF, CCCTC-binding factor; LE, Loop Extrusion model; MLL3/4, mixed-lineage leukemia protein ³/₄; Pol-II, RNA polymerase II; Pol-II-S2p, RNA polymerase II phosphorylated at Ser2; PRC2, Polycomb repressive complex 2; SBS, Strings&Binders model; TAD, topological associating domains.

as super-enhancers [12], hubs of interchromosomal interactions as those formed around the nucleolus or nuclear speckles [13], and interactions with the nuclear lamina where hundreds of large, gene repressive domains (named LADs) are formed [14]. Importantly, it has been discovered that large genomic mutations, in particular in noncoding regions, can interfere with the correct folding of DNA and, hence, alter the physical contacts between genes and their regulatory elements, thus resulting in severe human diseases, such as congenital disorders [15] and cancers [16,17]. Yet, the physical and molecular mechanisms shaping those contacts and controlling the functioning of the genome remain largely mysterious.

Here, we review the basic aspects of some of the quantitative models introduced from polymer physics to comprehend the physical mechanisms determining chromatin folding. We focus in particular on the Loop Extrusion model and the Strings&Binders phase separation model, and the scenario they depict of chromatin organization and gene regulation.

Chromatin organizing factors

Among the factors involved in the 3D organization of chromatin, CTCF binding sites and cohesin have been associated with the formation of loops and TADs [6] and linked to loop extrusion mechanisms [18-20]. Depletion of CTCF or cohesin leads indeed to loop release in bulk Hi-C data, albeit interactions signals persist at the compartment level and within former loops or TADs [21–23]. As mentioned, compartments A and B correlate to different transcriptional states [9], and homotypic interactions between active and poised gene promoters, associated, respectively, with Pol-II-S2p and PRC2, have been observed at the Mb scale and linked to phase separation mechanisms [24,25]. Indeed, physical mechanisms of phase separation are becoming a paradigm of cell organization [26,27] and of transcriptional control [28], as Pol-II, transcription factors, and coactivators, such as Mediator, have been shown to form condensates [29-32] involved in gene regulation [28,33–35].

Chromosomal contacts and TADs have a strong variability from cell to cell, as revealed by single-cell Hi-C experiments [36–39]. Additionally, multiplexed FISH microscopy approaches have shown that, while TAD-like globular 3D chromatin structures are present at the single-molecule level in single-cells, they are broadly varying from cell to cell [40–43]: for example, TAD boundaries can occur with nonzero probability at any genomic location and are enriched only at a subset of CTCF sites in the considered regions [42],

hinting that chromatin contacts could arise from mechanisms different from the loop extrusion.

Models of chromatin architecture from polymer physics

To make sense of the complexity of chromatin interaction data and explain the mode of action of their underlying molecular factors, two main models from polymer physics have been introduced to-date that are supported by growing experimental evidence. Here, we briefly review the key ingredients of those models, how they compare to experimental data and the emerging picture of the physical mechanisms underlying chromatin spatial organization.

The Loop Extrusion model (Fig. 1A) envisages that a molecular complex acts as an active motor extruding DNA loops between cognate anchor points, in a nonequilibrium process requiring energy influx by, e.g., ATP molecule consumption [18,19,44]. A different scenario, recapitulated by the Strings&Binders model (Fig. 1B), posits that chromatin interactions are mediated by diffusing cognate binding molecules, such as transcription factors (TFs), that can bridge pairs (or multiplets) of DNA sites via mechanisms of equilibrium polymer thermodynamics [24,26,45–60]. In such a scenario, DNA-molecule interactions induce chromatin structural changes via thermodynamics phase transitions, such as coil-to-globule or phase separation transitions, which spontaneously establish contacts or segregate specific, distal DNA sites, such as genes and enhancers.

It is also worth mentioning important computational approaches to reconstruct chromosome 3D conformations independent of the underlying physical processes, based on the optimization of scoring functions that compare contact data and inferred model 3D structures, albeit, for brevity, they are not discussed below [61–74].

The Loop Extrusion model

The core idea behind the *Loop Extrusion* (LE) Model [18,19,44] is that a loop-extruding factor, assumed to be cohesin, binds on DNA and actively extrudes a chromatin loop up to reach its extrusion blocking sites envisaged to be CTCF binding sites of opposite orientation (Fig. 1A). Eventually, the extrusion complex can dissociate from DNA and release the loop. The model details can be found in recent reviews [75]. From a physics point of view, the LE model describes an off-equilibrium process where an active motor (cohesin) burns energy, such as ATP, to extrude



Fig. 1. Polymer physics models of chromatin. (A) The Loop Extrusion (LE) model poses that a cohesin complex acts as an active motor extruding chromatin loops, whose anchor points along DNA are pairs of CTCF binding sites of opposite orientation [18,19,44]. A variant of the LE, the Slip-Link model [20], posits that cohesin becomes loaded at adjacent pairs of sites on the DNA chain and each of those sites can randomly slide, hence growing a loop, up to the anchor sites, with no energy inputs. The LE model is supported by a variety of important observations, and many experimental results can be successfully interpreted. (B) The Strings&Binders (SBS) model of chromatin considers the scenario where contacts between distal DNA regions are established by diffusing cognate binding factors [24,26]. A chromatin filament is modeled as a polymer chain and along the chain are located binding sites for different diffusing molecular binders. In the SBS model, chromatin contact patterns are established by a thermodynamics mechanism of globule phase separation. It has been shown to explain Hi-C, GAM, and FISH data across chromosomal scales and cell types [24,25,49,57] and has been validated by predicting the impact of disease-linked mutations on the 3D structure of DNA [46,93,97]. (C) The genomic location of the binding sites of the model of a locus of interest can be derived by epigenetic and TF Chip-seq data. (D) Alternatively, they can be inferred by a Machine Learning procedure (PRISMR, [46]) that searches the minimal set of binding sites that, based only on physics, folds the polymer to best match input bulk Hi-C data. (E) An ensemble of single-molecule 3D structures of chromatin can be derived by Molecular Dynamics computer simulations from the inferred linear polymer model of the investigated loci [88]. Computer simulations also permit to access the real time dynamics of chromatin, e.g., how contact patterns are established and change in time or under different conditions.

chromatin loops. The *Slip-Link* model is a variant of the LE where extrusion occurs driven by thermal diffusion, without requiring an energy burning motor [20]. Various choices of the model different parameters can reproduce patterns of contact data beyond point-wise interactions between the loop anchor points, such as TADs and lines of enriched contacts between a CTCF site and a flanking region, features typically visible in Hi-C data.

The loop extrusion model has been invoked to explain experiments, for instance, on mitotic chromosome compaction and segregation [76], meiotic chromosome organization in *S. cerevisiae* [77] and V(D)J recombination [78,79].

Importantly, a direct experimental observation of the motor activity of factors such as condensin and cohesin in extruding DNA loops has been recently provided by *in vitro* single-molecule experiments, albeit in simplified conditions, giving evidence in favor of the loop extrusion mechanism [80–83]. In addition to giving a natural interpretation to the CTCF convergence bias in loops visible in Hi-C data, indirect support of the LE model is also found in important experiments where perturbation of CTCF or cohesin affect chromatin organization. For example, disruption of specific CTCF binding sites produces architectural rearrangements in agreement with LE [18,84,85]. Also, genomewide cohesin or CTCF degron leads to massive disappearance of TADs and loops [21–23,86].

However, bulk Hi-C data produced in CTCF or cohesin depletion experiments reveal also that interactions persist at the A/B compartment level and within former loops or TADs [21–23]. Additionally, multiplexed FISH microscopy has shown that in single-cells TAD-like domains are broadly varying [40–43] and TAD boundaries can occur with nonzero probability at any genomic location, not just at a subset of CTCF sites [42]. Those important experiments provide evidence that chromatin 3D architecture is only partially dependent on CTCF/cohesin and arises also from mechanisms different from the loop extrusion.

The Strings&Binders model

Another class of polymer models of chromatin architecture has explored the picture where specific interactions exist between different types of distal DNA binding sites, either arising by direct contact or established by diffusing molecules, such as transcription factors (TFs), that bridge those sites, hence producing DNA loops [24,26,45–60]. Those models investigate the emergent structural properties of the system, derived by polymer thermodynamics, and form a broad class of universality, as dictated by Statistical Mechanics. Here we focus on a well-known example within this class, the Strings&Binders model (SBS) [26] (Fig. 1B), which has been broadly applied to investigate chromatin structure at the single-molecule level in wild-type genomes and to understand the impact of disease-associated mutations. In the SBS model, a chromatin filament is represented as a self-avoidingwalk polymer having specific as well as unspecific binding sites for cognate, diffusing molecular binders [24,26]. Driven by thermodynamics, above a threshold concentration the binders stably bridge their cognate sites, thus forming loops and defining the system architecture.

The core idea of the SBS model is that, as dictated by polymer physics [87], the system equilibrium 3D conformations fall in just a few folding classes corresponding to its thermodynamics phases, which can be predicted by physics. For example, as the number of binders (or affinity strength) grows above a threshold point, the system typically undergoes a phase transition from a coil, randomly folded state to a globular, more compact state. Hence, by determining the system thermodynamics phases one can derive the full ensemble of 3D conformations where it spontaneously folds into. Note that in a given thermodynamic state, i.e., for a given binder concentration, the system can fold in a variety of 3D conformations, not just in a unique, naive structure, so resulting in a broad variability of single-molecule architectures. The model details can be found in recent reviews [88,89].

To derive the specific architecture of a genomic region of interest, it is necessary to identify the specific genomic location and the types of the binding sites of the polymer model of such a region (Fig. 1C, D). A typical approach exploits prior knowledge of epigenetic or TFs Chip-seq signals (Fig. 1C). Indeed, a number of molecular factors has been discovered to have a role in chromosome architecture, encompassing a variety of TFs and epigenetic tracks, such as CTCF/Cohesin [18], MLL3/4 [90], polycomb repressive complex 1 [91], active and poised Pol-II [25]. The model is informed with such known binding sites and, next, its 3D conformations are derived by Molecular Dynamics simulations (Fig. 1E) [45,47–49,51,56–58,60]. The advantage of such an approach is that different scenarios can be tested to understand the nature of the key factors shaping the architecture, yet a limitation is that only known factors can be considered. A different approach (Fig. 1D) exploits a machine learning procedure whereby from only contact data, say Hi-C data, the minimal set of putative model binding sites is inferred which best explains, out of only physics, the input data with no additional prior knowledge [46,50,59]. Next, to learn the molecular nature of the inferred model binding sites, their genomic position is correlated with available information on chromatin organizing factors in the same cell type. Note that usually a single binding site type must not be identified with a single molecular factor; conversely, it has been shown that different binders typically correlate with distinct combinations of factors [45]. Such a method is advantageous to avoid biases toward a subset of TFs in explaining contact data and to discover novel combinations of molecular elements or new putative factors that control folding.

The SBS model has been used to understand the 3D conformations of a number of loci, such as the HoxB



Fig. 2. Single-molecule 3D structures derived by globule phase separation within the SBS model can explain single-cell multiplexed FISH microscopy data. (A) The single-molecule conformations derived by SBS model of a human locus in HCT116 cells [50] match very well single-cell microscopy data from multiplexed FISH experiments [42]. The mechanism underlying globule formation was traced back to polymer phase separation, whereas the variability of single-molecule conformations results from the intrinsic degeneracy of the system thermodynamic microstates. (B) The model comparison with experimental data of the same locus in cohesin depleted cells shows that phase separation is reversed back into random coil conformations, erasing average patterns [50]. Interestingly, recent experiments have shown that cohesin does phase separates into aggregates with DNA in an ATP-independent manner [52].

[25], HoxD [92], Shh [93], or alpha/beta-globin locus [94]. It has also been employed to shed light on the architectural rearrangements upon differentiation of those loci, as cell type- and gene-specific multiway contacts are established with regulatory elements in connection to epigenetic and transcriptional changes [25,92,94,95]. Models of interacting polymers, in the same class of the SBS, have been successfully employed to explain TAD and contact pattern formation also at chromosomal scales [45,48,57,96], to explore structural heterogeneity at the single-molecule level [47,51], and to dissect Hi-C data in a variety of loci, chromosomes and organisms, such as yeast, Drosophila, murine, and human cells [40,56,58]. A limitation of this type of models is that they need additional ingredients to explain the CTCF convergence bias of loops, which is instead naturally included within the LE framework. In this direction, models combining both LE and affinity-based (e.g. SBS) mechanisms have been shown to describe well chromatin folding data [21,47,49].

The SBS model has been also important to investigate the mechanisms underlying the formation of

of specific loci [25,59], and its predictions have been validated against single-cell imaging data [50]. Those studies have provided evidence that chromatin TADlike globules, revealed by microscopy experiments (see, e.g., [42]), are established by a thermodynamics mechanism of polymer phase separation [50]. The distinct globules self-assemble by the combinatorial action of different chromatin organizing factors, including, but not limited to CTCF and cohesin. Those globules define stable environments where specific contacts between cognate regions (e.g., gene-enhancers) are favored over stochastic encounters. That is a robust, reversible mechanism of spatial organization, where stochasticity and specificity co-exist. In particular, the broad cell-to-cell variability of 3D structures naturally emerges from the thermodynamic degeneracy of conformations predicted by the theory. Applications to cohesin depleted cells have shown that cohesin depletion reverses phase separation into randomly folded states, hence erasing average interaction patterns [50], in agreement with recent experiments that have confirmed that cohesin shows pronounced clustering on

TADs at the single-molecule level (Fig. 2) in a variety



Fig. 3. The SBS model predicts how structural variants rewire gene-enhancers contacts. (A) The SBS model of a genomic region can be used to make predictions on the impact of large mutations, such as structural variants, on the locus architecture and, in particular, on the rewiring of regulatory contacts between genes and enhancers (enhancer-hijacking). (B) The shown examples concern the human EPHA4 locus, where different mutations are associated with different limb malformations. The SBS model predictions are all confirmed by independent cHi-C experiments, providing insights on the mechanisms whereby ectopic gene activation is induced and the phenotype developed [46].

DNA, in an ATP-independent manner, typical of phase separation [52].

The predictive power of the SBS model to reconstruct the impact on the 3D architecture of large mutations (Structural variants) linked to human diseases has been successfully tested against experiments in different cell types and loci, such as the human EPHA4 [46], Pitx1 [97], and Shh [93] loci. In particular, the model was used to predict how those mutations rewire the contacts between genes and their regulators (*enhancer-hijacking*) hence activating ectopic transcription that leads to disease, and how different mutations induce distinct enhancer-hijackings and phenotypes (Fig. 3). It was also used to show how 3D conformation determines enhancer tissue specificity and morphogenic identity [97].

Concluding remarks and perspectives

As the wealth and complexity of experimental data are growing, models from polymer physics are becoming essential to dissect the mechanisms underlying chromosome spatial organization and its functional implications. We focused, in particular, on the scenarios depicted by the Loop Extrusion and Strings&Binders polymer models, which are supported by a number of recent experiments.

DNA loop extrusion has emerged as an important mechanism of chromatin organization [75], posing that a cohesin linked active motor extrudes loops between CTCF anchor points, in a nonequilibrium, active process. The extruding motor activity of cohesin has been recently also experimentally confirmed in vitro [81,82] and its role in chromatin architecture supported by bulk Hi-C data in systems depleted for CTCF or cohesin [21-23]. However, super-resolution single-cell imaging experiments in human loci have shown that DNA interactions can arise from other important molecular process [42], consistent with a folding mechanism based on polymer phase separation as depicted by the Strings&Binders model [24,50]. Intriguingly, novel experiments in yeast have shown that cohesin also phase separates into aggregates with DNA in an ATPindependent manner [52].

The models we discussed appear to return a simplified description of the molecular complexity of real chromatin, yet they may capture real features of chromosome folding because of the Statistical Mechanics concept of universality in phase transitions [87], whereby stylized models can exhibit the same emergent features of their more detailed and refined counterparts. Yet, more faithful molecular representations of chromatin can reveal a variety of additional specific properties, which could be relevant to different biological situations. Additionally, it remains to be clarified under which circumstances loop extrusion can proceed on real chromatin *in vivo* in the complex environment of the nucleoplasm or, within the SBS model scenario, how near equilibrium can be reached.

Nevertheless, the Loop Extrusion model appears to be a basic chromatin organizational mechanism, which can be implemented by active motors as well as by diffusion, as in its Slip-Link variant. And thermodynamics phase transitions and self-assembling, as those described by the Strings&Binders model, are reliable and reversible mechanisms to control conformations, requiring no energy input beyond the thermal bath. Importantly, phase transition mechanisms require no molecular fine-tuning as the system can be transited in a different structural phase by basic cell processes, such as up-regulation of TFs or epigenetic factors [26]. However, other folding mechanisms, yet to be discovered, are likely to play a role in establishing chromatin architecture, and in different chromosomal regions, different physical processes could contribute or co-exist.

Importantly, models from polymer physics are providing a deeper understanding of the 3D organization of the genome and how it is altered by mutations linked to phenotypes, relevant to congenital disorders [15] or cancer [16,17,98]. In this regard, recent analysis on thousands of cancer genomes [99] involving several tumor types, identified structural variation as one of the key mutational processes in cancer [100] highlighting even more the deep connection between chromatin 3D architecture and disease. Hence, the strategic combination of quantitative models and advanced experimental technologies can help opening new routes to design strategies to attack diseases linked to genomic architectural modifications.

Acknowledgements

M.N. acknowledges support from the NIH 4D Nucle-Program grant 1U54DK107977-01 and ome 1UM1HG011585-01 and the EU H2020 Marie Curie ITN n.813282, Einstein BIH Fellowship Award (EVF-BIH-2016-282 and 2019), CINECA ISCRA ID HP10CYFPS5 and HP10CRTY8P, Regione Campania POR SATIN 2018-2020. S.B. and A.M.C. acknowledge support from the CINECA ISCRA grant ID HP10CCZ4KN. We acknowledge computer resources from INFN, CINECA, ENEA CRESCO/ENEAGRID (Ponti et al., 2014) and Scope/ReCAS/Ibisco at the University of Naples.

Conflict of interest

The authors declare no conflict of interest.

Author contributions

AMC, SB, and MN wrote the manuscript with inputs from the other authors.

References

- Sigal YM, Zhou R & Zhuang X (2018) Visualizing and discovering cellular structures with super-resolution microscopy. *Science* 361, 880–887.
- 2 Kempfer R & Pombo A (2020) Methods for mapping 3D chromosome architecture. *Nat Rev Genet* **21**, 207– 226.
- 3 Dekker J & Mirny L (2016) The 3D genome as moderator of chromosomal communication. *Cell* 164, 1110–1121.
- 4 Dixon JR, Gorkin DU & Ren B (2016) Chromatin domains: the unit of chromosome organization. *Mol Cell* **62**, 668–680.
- 5 Finn EH & Misteli T (2019) Molecular basis and biological function of variability in spatial genome organization. *Science* **365**, eaaw9498.
- 6 Rao SSP, Huntley MH, Durand NC, Stamenova EK, Bochkov ID, Robinson JT, Sanborn AL, Machol I, Omer AD, Lander ES & *et al*, (2014) A 3D map of the human genome at kilobase resolution reveals principles of chromatin looping. *Cell* **159**, 1665–1680.
- 7 Nora EP, Lajoie BR, Schulz EG, Giorgetti L, Okamoto I, Servant N, Piolot T, Van Berkum NL, Meisig J, Sedat J *et al*, (2012) Spatial partitioning of the regulatory landscape of the X-inactivation centre. *Nature* 485, 381–385.
- 8 Dixon JR, Selvaraj S, Yue F, Kim A, Li Y, Shen Y, Hu M, Liu JS & Ren B (2012) Topological domains in mammalian genomes identified by analysis of chromatin interactions. *Nature* 485, 376–380.
- 9 Lieberman-Aiden E, Van Berkum NL, Williams L, Imakaev M, Ragoczy T, Telling A, Amit I, Lajoie BR, Sabo PJ, Dorschner MO *et al*, (2009) Comprehensive mapping of long-range interactions reveals folding principles of the human genome. *Science* **326**, 289–293.
- Phillips-Cremins JE, Sauria MEG, Sanyal A, Gerasimova TI, Lajoie BR, Bell JSK, Ong CT, Hookway TA, Guo C, Sun Y *et al*, (2013) Architectural protein subclasses shape 3D organization of genomes during lineage commitment. *Cell* 153, 1281–1295.
- 11 Fraser J, Ferrai C, Chiariello AM, Schueler M, Rito T, Laudanno G, Barbieri M, Moore BL, Kraemer DC, Aitken S *et al*, (2015) Hierarchical folding and reorganization of chromosomes are linked to

transcriptional changes in cellular differentiation. *Mol Syst Biol* **11**, 852.

- 12 Beagrie RA, Scialdone A, Schueler M, Kraemer DCA, Chotalia M, Xie SQ, Barbieri M, De Santiago I, Lavitas LM, Branco MR *et al*, (2017) Complex multienhancer contacts captured by genome architecture mapping. *Nature* 543, 519–524.
- 13 Quinodoz SA, Ollikainen N, Tabak B, Palla A, Schmidt JM, Detmar E, Lai MM, Shishkin AA, Bhat P, Takei Y *et al*, (2018) Higher-order interchromosomal hubs shape 3D genome organization in the nucleus. *Cell* **174**, 744–757.e24.
- 14 van Steensel B & Belmont AS (2017) Laminaassociated domains: links with chromosome architecture, heterochromatin, and gene repression. *Cell* 169, 780–791.
- 15 Spielmann M, Lupiáñez DG & Mundlos S (2018) Structural variation in the 3D genome. *Nat Rev Genet* 19, 453–467.
- 16 Valton AL & Dekker J (2016) TAD disruption as oncogenic driver. Curr Opin Genet Dev 36, 34–40.
- 17 Weischenfeldt J, Dubash T, Drainas AP, Mardin BR, Chen Y, Stütz AM, Waszak SM, Bosco G, Halvorsen AR, Raeder B *et al*, (2017) Pan-cancer analysis of somatic copy-number alterations implicates IRS4 and IGF2 in enhancer hijacking. *Nat Genet* **49**, 65–74.
- 18 Sanborn AL, Rao SSP, Huang S-C, Durand NC, Huntley MH, Jewett AI, Bochkov ID, Chinnappan D, Cutkosky A, Li J *et al*, (2015) Chromatin extrusion explains key features of loop and domain formation in wild-type and engineered genomes. *Proc Natl Acad Sci* 112, E6456–E6465.
- 19 Fudenberg G, Imakaev M, Lu C, Goloborodko A, Abdennur N & Mirny LA (2016) Formation of chromosomal domains by loop extrusion. *Cell Rep* 15, 2038–2049.
- 20 Brackley CA, Johnson J, Michieletto D, Morozov AN, Nicodemi M, Cook PR & Marenduzzo D (2017) Nonequilibrium chromosome looping via molecular slip links. *Phys Rev Lett* **119**, 138101.
- 21 Rao SSP, Huang SC, Glenn St Hilaire B, Engreitz JM, Perez EM, Kieffer-Kwon KR, Sanborn AL, Johnstone SE, Bascom GD, Bochkov ID *et al*, (2017) Cohesin loss eliminates all loop domains. *Cell* **171**, 305–320.e24.
- 22 Schwarzer W, Abdennur N, Goloborodko A, Pekowska A, Fudenberg G, Loe-Mie Y, Fonseca NA, Huber W, Haering CH, Mirny L & *et al*, (2017) Two independent modes of chromatin organization revealed by cohesin removal. *Nature* 551, 51–56.
- 23 Nora EP, Goloborodko A, Valton A-L, Gibcus JH, Uebersohn A, Abdennur N, Dekker J, Mirny LA & Bruneau BG (2017) Targeted degradation of CTCF decouples local insulation of chromosome domains from genomic compartmentalization. *Cell* 169, 930– 944.e22.

- 24 Barbieri M, Chotalia M, Fraser J, Lavitas L-M, Dostie J, Pombo A & Nicodemi M (2012) Complexity of chromatin folding is captured by the strings and binders switch model. *Proc Natl Acad Sci* 109, 16173– 16178.
- 25 Barbieri M, Xie SQ, Torlai Triglia E, Chiariello AM, Bianco S, De Santiago I, Branco MR, Rueda D, Nicodemi M & Pombo A (2017) Active and poised promoter states drive folding of the extended HoxB locus in mouse embryonic stem cells. *Nat Struct Mol Biol* 24, 515–524.
- 26 Nicodemi M & Prisco A (2009) Thermodynamic pathways to genome spatial organization in the cell nucleus. *Biophys J* 96, 2168–2177.
- 27 Shin Y & Brangwynne CP (2017) Liquid phase condensation in cell physiology and disease. *Science* 357, eaaf4382.
- 28 Hnisz D, Shrinivas K, Young RA, Chakraborty AK & Sharp PA (2017) A phase separation model for transcriptional control. *Cell* 169, 13–23.
- 29 Boija A, Klein IA, Sabari BR, Dall'Agnese A, Coffey EL, Zamudio AV, Li CH, Shrinivas K, Manteiga JC, Hannett NM *et al*, (2018) Transcription factors activate genes through the phase-separation capacity of their activation domains. *Cell* 175, 1842–1855.e16.
- 30 Cho W-K, Spille J-H, Hecht M, Lee C, Li C, Grube V & Cisse II (2018) Mediator and RNA polymerase II clusters associate in transcription-dependent condensates. *Science* 361, 412–415.
- 31 Sabari BR, Dall'Agnese A, Boija A, Klein IA, Coffey EL, Shrinivas K, Abraham BJ, Hannett NM, Zamudio AV, Manteiga JC *et al*, (2018) Coactivator condensation at super-enhancers links phase separation and gene control. *Science* 361, eaar3958.
- 32 Chong S, Dugast-Darzacq C, Liu Z, Dong P, Dailey GM, Cattoglio C, Heckert A, Banala S, Lavis L, Darzacq X & et al, (2018) Imaging dynamic and selective low-complexity domain interactions that control gene transcription. Science 361, eaar2555.
- 33 Larson AG, Elnatan D, Keenen MM, Trnka MJ, Johnston JB, Burlingame AL, Agard DA, Redding S & Narlikar GJ (2017) Liquid droplet formation by HP1α suggests a role for phase separation in heterochromatin. *Nature* 547, 236–240.
- 34 Strom AR, Emelyanov AV, Mir M, Fyodorov DV, Darzacq X & Karpen GH (2017) Phase separation drives heterochromatin domain formation. *Nature* 547, 241–245.
- 35 Guo YE, Manteiga JC, Henninger JE, Sabari BR, Agnese A, Hannett NM, Spille J-H, Afeyan LK, Zamudio AV, Shrinivas K *et al*, (2019) Pol II phosphorylation regulates a switch between transcriptional and splicing condensates. *Nature* 572, 543–548.

- 36 Nagano T, Lubling Y, Stevens TJ, Schoenfelder S, Yaffe E, Dean W, Laue ED, Tanay A & Fraser P (2013) Single-cell Hi-C reveals cell-to-cell variability in chromosome structure. *Nature* **502**, 59–64.
- 37 Flyamer IM, Gassler J, Imakaev M, Brandão HB, Ulianov SV, Abdennur N, Razin SV, Mirny LA & Tachibana-Konwalski K (2017) Single-nucleus Hi-C reveals unique chromatin reorganization at oocyte-tozygote transition. *Nature* 544, 110–114.
- 38 Stevens TJ, Lando D, Basu S, Atkinson LP, Cao Y, Lee SF, Leeb M, Wohlfahrt KJ, Boucher W, O'Shaughnessy-Kirwan A *et al*, (2017) 3D structures of individual mammalian genomes studied by singlecell Hi-C. *Nature* 544, 59–64.
- 39 Nagano T, Lubling Y, Várnai C, Dudley C, Leung W, Baran Y, Mendelson Cohen N, Wingett S, Fraser P & Tanay A (2017) Cell-cycle dynamics of chromosomal organization at single-cell resolution. *Nature* 547, 61– 67.
- 40 Boettiger AN, Bintu B, Moffitt JR, Wang S, Beliveau BJ, Fudenberg G, Imakaev M, Mirny LA, Wu C & Zhuang X (2016) Super-resolution imaging reveals distinct chromatin folding for different epigenetic states. *Nature* 529, 418–422.
- 41 Cattoni DI, Cardozo Gizzi AM, Georgieva M, Di Stefano M, Valeri A, Chamousset D, Houbron C, Déjardin S, Fiche J-B, González I *et al*, (2017) Single-cell absolute contact probability detection reveals chromosomes are organized by multiple lowfrequency yet specific interactions. *Nat Commun* 8, 1753.
- 42 Bintu B, Mateo LJ, Su J-H, Sinnott-Armstrong NA, Parker M, Kinrot S, Yamaya K, Boettiger AN & Zhuang X (2018) Super-resolution chromatin tracing reveals domains and cooperative interactions in single cells. *Science* 362, eaau1783.
- 43 Cardozo Gizzi AM, Cattoni DI, Fiche J-B, Espinola SM, Gurgo J, Messina O, Houbron C, Ogiyama Y, Papadopoulos GL, Cavalli G *et al*, (2019) Microscopybased chromosome conformation capture enables simultaneous visualization of genome organization and transcription in intact organisms. *Mol Cell* 74, 212– 222.e5.
- 44 Goloborodko A, Marko JF & Mirny LA (2016) Chromosome compaction by active loop extrusion. *Biophys J* 110, 2162–2168.
- 45 Di Pierro M, Zhang B, Aiden EL, Wolynes PG & Onuchic JN (2016) Transferable model for chromosome architecture. *Proc Natl Acad Sci* **113**, 12168–12173.
- 46 Bianco S, Lupiáñez DG, Chiariello AM, Annunziatella C, Kraft K, Schöpflin R, Wittler L, Andrey G, Vingron M, Pombo A *et al*, (2018) Polymer physics predicts the effects of structural variants on chromatin architecture. *Nat Genet* **50**, 662–667.

- 47 Buckle A, Brackley CA, Boyle S, Marenduzzo D & Gilbert N (2018) Polymer simulations of heteromorphic chromatin predict the 3d folding of complex genomic loci. *Mol Cell* **72**, 786–797.e11.
- 48 Shi G, Liu L, Hyeon C & Thirumalai D (2018) Interphase human chromosome exhibits out of equilibrium glassy dynamics. *Nat Commun* 9, 3161.
- 49 Nuebler J, Fudenberg G, Imakaev M, Abdennur N & Mirny LA (2018) Chromatin organization by an interplay of loop extrusion and compartmental segregation. *Proc Natl Acad Sci* 115, E6697–E6706.
- 50 Conte M, Fiorillo L, Bianco S, Chiariello AM, Esposito A & Nicodemi M (2020) Polymer physics indicates chromatin folding variability across singlecells results from state degeneracy in phase separation. *Nat Commun* 11, 3289.
- 51 Cheng RR, Contessoto V, Aiden EL, Wolynes PG, Di PM & Onuclhic JN (2020) Exploring Chromosomal Structural Heterogeneity Across Multiple Cell Lines. *BioRxiv*. https://doi.org/10.1101/2020.03.21.001917.
- 52 Ryu J-K, Bouchoux C, Liu HW, Kim E, Minamino M, de Groot R, Katan AJ, Bonato A, Marenduzzo D, Michieletto D *et al*, (2020) Phase separation induced by cohesin SMC protein complexes. *BioRxiv*. [PREPRINT] https://doi.org/10.1101/2020.06.13. 149716.
- 53 Odenheimer J, Kreth G & Heermann DW (2005) Dynamic Simulation of Active/Inactive Chromatin Domains. J Biol Phys 31, 351–363.
- 54 Bohn M & Heermann DW (2010) Diffusion-Driven Looping Provides a Consistent Framework for Chromatin Organization. *PLoS One* 5, e12218.
- 55 Brackley CA, Taylor S, Papantonis A, Cook PR & Marenduzzo D (2013) Nonspecific bridging-induced attraction drives clustering of DNA-binding proteins and genome organization. *Proc Natl Acad Sci U S A* **110**, E3605–E3611.
- 56 Jost D, Carrivain P, Cavalli G & Vaillant C (2014) Modeling epigenome folding: Formation and dynamics of topologically associated chromatin domains. *Nucleic Acids Res* 42, 9553–9561.
- 57 Zhang B & Wolynes PG (2015) Topology, structures, and energy landscapes of human chromosomes. *Proc Natl Acad Sci* **112**, 6062–6067.
- 58 Brackley CA, Brown JM, Waithe D, Babbs C, Davies J, Hughes JR, Buckle VJ & Marenduzzo D (2016) Predicting the three-dimensional folding of cisregulatory regions in mammalian genomes using bioinformatic data and polymer models. *Genome Biol* 17, 59.
- 59 Chiariello AM, Annunziatella C, Bianco S, Esposito A & Nicodemi M (2016) Polymer physics of chromosome large-scale 3D organisation. *Sci Rep* 6, 29775.
- 60 Di Stefano M, Paulsen J, Lien TG, Hovig E & Micheletti C (2016) Hi-C-constrained physical models

of human chromosomes recover functionally-related properties of genome organization. *Sci Rep* **6**, 35985.

- 61 Duan Z, Andronescu M, Schutz K, McIlwain S, Kim YJ, Lee C, Shendure J, Fields S, Blau CA & Noble WS (2010) A three-dimensional model of the yeast genome. *Nature* 465, 363–367.
- 62 Baú D, Sanyal A, Lajoie BR, Capriotti E, Byron M, Lawrence JB, Dekker J & Marti-Renom MA (2011) The three-dimensional folding of the α-globin gene domain reveals formation of chromatin globules. *Nat Struct Mol Biol* 18, 107–115.
- 63 Serra F, Baù D, Goodstadt M, Castillo D, Filion GJ & Marti-Renom MA (2017) Automatic analysis and 3D-modelling of Hi-C data using TADbit reveals structural features of the fly chromatin colors. *PLOS Comput Biol* 13, e1005665.
- 64 Nir G, Farabella I, Pérez Estrada C, Ebeling CG, Beliveau BJ, Sasaki HM, Lee SD, Nguyen SC, McCole RB, Chattoraj S *et al*,(2018) Walking along chromosomes with super-resolution imaging, contact maps, and integrative modeling. *PLOS Genet* 14, e1007872.
- 65 Hua N, Tjong H, Shin H, Gong K, Zhou XJ & Alber F (2018) Producing genome structure populations with the dynamic and automated PGS software. *Nat Protoc* 13, 915–926.
- 66 Lin D, Bonora G, Yardımcı GG & Noble WS (2019) Computational methods for analyzing and modeling genome structure and organization. *Wiley Interdiscip Rev Syst Biol Med* **11**, e1435.
- 67 Rousseau M, Fraser J, Ferraiuolo MA, Dostie J & Blanchette M (2011) Three-dimensional modeling of chromatin structure from interaction frequency data using Markov chain Monte Carlo sampling. *BMC Bioinformatics* 12, 414.
- 68 Kalhor R, Tjong H, Jayathilaka N, Alber F & Chen L (2012) Genome architectures revealed by tethered chromosome conformation capture and populationbased modeling. *Nat Biotechnol* **30**, 90–98.
- 69 Peng C, Fu L-Y, Dong P-F, Deng Z-L, Li J-X, Wang X-T & Zhang H-Y (2013) The sequencing bias relaxed characteristics of Hi-C derived data and implications for chromatin 3D modeling. *Nucleic Acids Res* **41**, e183.
- 70 Zhang Z, Li G, Toh K-C & Sung W-K (2013) 3D Chromosome Modeling with Semi-Definite Programming and Hi-C Data. *J Comput Biol* 20, 831– 846.
- 71 Hu M, Deng K, Qin Z, Dixon J, Selvaraj S, Fang J, Ren B & Liu JS (2013) Bayesian Inference of Spatial Organizations of Chromosomes. *PLoS Comput Biol* 9, e1002893.
- 72 Varoquaux N, Ay F, Noble WS & Vert J-P (2014) A statistical approach for inferring the 3D structure of the genome. *Bioinformatics* **30**, i26–i33.

- 73 Lesne A, Riposo J, Roger P, Cournac A & Mozziconacci J (2014) 3D genome reconstruction from chromosomal contacts. *Nat Methods* 11, 1141–1143.
- 74 Tjong H, Li W, Kalhor R, Dai C, Hao S, Gong K, Zhou Y, Li H, Zhou XJ, Le Gros MA *et al*, (2016) Population-based 3D genome structure analysis reveals driving forces in spatial genome organization. *Proc Natl Acad Sci USA* **113**, E1663–E1672.
- 75 Banigan EJ & Mirny LA (2020) Loop extrusion: theory meets single-molecule experiments. *Curr Opin Cell Biol* 64, 124–138.
- 76 Gibcus JH, Samejima K, Goloborodko A, Samejima I, Naumova N, Nuebler J, Kanemaki MT, Xie L, Paulson JR, Earnshaw WC *et al*, (2018) A pathway for mitotic chromosome formation. *Science* 359, eaao6135.
- 77 Schalbetter SA, Fudenberg G, Baxter J, Pollard KS & Neale MJ (2019) Principles of meiotic chromosome assembly revealed in S. cerevisiae. *Nat Commun* 10, 4795.
- 78 Zhang Y, Zhang X, Ba Z, Liang Z, Dring EW, Hu H, Lou J, Kyritsis N, Zurita J, Shamim MS *et al*, (2019) The fundamental role of chromatin loop extrusion in physiological V(D)J recombination. *Nature* **573**, 600– 604.
- 79 Hill L, Ebert A, Jaritz M, Wutz G, Nagasaka K, Tagoh H, Kostanova-Poliakova D, Schindler K, Sun Q, Bönelt P *et al*, (2020) Wapl repression by Pax5 promotes V gene recombination by Igh loop extrusion. *Nature* 584, 142–147.
- 80 Ganji M, Shaltiel IA, Bisht S, Kim E, Kalichava A, Haering CH & Dekker C (2018) Real-time imaging of DNA loop extrusion by condensin. *Science* 360, 102– 105.
- 81 Kim Y, Shi Z, Zhang H, Finkelstein IJ & Yu H (2019) Human cohesin compacts DNA by loop extrusion. *Science* 366, 1345–1349.
- 82 Davidson IF, Bauer B, Goetz D, Tang W, Wutz G & Peters J-M (2019) DNA loop extrusion by human cohesin. *Science* 366, 1338–1345.
- 83 Kong M, Cutts EE, Pan D, Beuron F, Kaliyappan T, Xue C, Morris EP, Musacchio A, Vannini A & Greene EC (2020) Human Condensin I and II Drive Extensive ATP-Dependent Compaction of Nucleosome-Bound DNA. *Mol Cell* **79**, 99–114.e9.
- 84 Guo Y, Xu Q, Canzio D, Shou J, Li J, Gorkin DU, Jung I, Wu H, Zhai Y, Tang Y *et al*, (2015) CRISPR Inversion of CTCF Sites Alters Genome Topology and Enhancer/Promoter Function. *Cell* 162, 900–910.
- 85 de Wit E, Vos ESM, Holwerda SJB, Valdes-Quezada C, Verstegen MJAM, Teunissen H, Splinter E, Wijchers PJ, Krijger PHL & de Laat W (2015) CTCF binding polarity determines chromatin looping. *Mol Cell* **60**, 676–684.
- 86 Vian L, Pękowska A, Rao SSP, Kieffer-Kwon K-R, Jung S, Baranello L, Huang S-C, El Khattabi L, Dose

M, Pruett N *et al*, (2018) The Energetics and Physiological Impact of Cohesin Extrusion. *Cell* **173**, 1165–1178.e20.

- 87 De Gennes PG (1979) Scaling concepts in polymer physics. Cornell University Press, Ithaca, NY.
- 88 Annunziatella C, Chiariello AM, Esposito A, Bianco S, Fiorillo L & Nicodemi M (2018) Molecular dynamics simulations of the strings and Binders Switch model of chromatin. *Methods* 142, 81–88.
- 89 Bianco S, Chiariello AM, Conte M, Esposito A, Fiorillo L, Musella F & Nicodemi M (2020) Computational approaches from polymer physics to investigate chromatin folding. *Curr Opin Cell Biol* 64, 10–17.
- 90 Yan J, Chen S-AA, Local A, Liu T, Qiu Y, Dorighi KM, Preissl S, Rivera CM, Wang C, Ye Z *et al*, (2018) Histone H3 lysine 4 monomethylation modulates longrange chromatin interactions at enhancers. *Cell Res* 28, 204–220.
- 91 Kundu S, Ji F, Sunwoo H, Jain G, Lee JT, Sadreyev RI, Dekker J & Kingston RE (2017) Polycomb repressive complex 1 generates discrete compacted domains that change during differentiation. *Mol Cell* 65, 432–446.e5.
- 92 Bianco S, Annunziatella C, Andrey G, Chiariello AM, Esposito A, Fiorillo L, Prisco A, Conte M, Campanile R & Nicodemi M (2019) Modeling single-molecule conformations of the HoxD region in mouse embryonic stem and cortical neuronal cells. *Cell Rep* 28, 1574–1583.e4.
- 93 Paliou C, Guckelberger P, Schöpflin R, Heinrich V, Esposito A, Chiariello AM, Bianco S, Annunziatella C, Helmuth J, Haas S *et al*, (2019) Preformed chromatin topology assists transcriptional robustness of Shh during limb development. *Proc Natl Acad Sci* 116, 12390–12399.

- 94 Chiariello AM, Bianco S, Oudelaar AM, Esposito A, Annunziatella C, Fiorillo L, Conte M, Corrado A, Prisco A, Larke MSC *et al*, (2020) A dynamic folded hairpin conformation is associated with α-globin activation in erythroid cells. *Cell Rep* **30**, 2125–2135.e5.
- 95 Oudelaar AM, Davies JOJ, Hanssen LLP, Telenius JM, Schwessinger R, Liu Y, Brown JM, Downes DJ, Chiariello AM, Bianco S *et al*, (2018) Single-allele chromatin interactions identify regulatory hubs in dynamic compartmentalized domains. *Nat Genet* **50**, 1744–1751.
- 96 Johnstone SE, Reyes A, Qi Y, Adriaens C, Hegazi E, Pelka K, Chen JH, Zou LS, Drier Y, Hecht V *et al*, (2020) Large-Scale topological changes restrain malignant progression in colorectal cancer. *Cell* 182, 1474–1489.e23.
- 97 Kragesteen BK, Spielmann M, Paliou C, Heinrich V, Schöpflin R, Esposito A, Annunziatella C, Bianco S, Chiariello AM, Jerković I *et al*, (2018) Dynamic 3D chromatin architecture contributes to enhancer specificity and limb morphogenesis. *Nat Genet* 50, 1463–1473.
- 98 Dellino GI, Palluzzi F, Chiariello AM, Piccioni R, Bianco S, Furia L, De Conti G, Bouwman BAM, Melloni G, Guido D *et al*, (2019) Release of paused RNA polymerase II at specific loci favors DNA double-strand-break formation and promotes cancer translocations. *Nat Genet* **51**, 1011–1023.
- 99 The ICGC/TCGA Pan-Cancer Analysis of Whole Genomes Consortium (2020) Pan-cancer analysis of whole genomes. *Nature* 578, 82–93.
- 100 Li Y, Roberts ND, Wala JA, Shapira O, Schumacher SE, Kumar K, Khurana E, Waszak S, Korbel JO, Haber JE *et al*, (2020) Patterns of somatic structural variation in human cancer genomes. *Nature* **578**, 112– 121.