

Sensitivity analysis for an elemental sulfur-based two-step denitrification model

A. Kostrytsia, S. Papirio, M. R. Mattei, L. Frunzo, P. N. L. Lens and G. Esposito

ABSTRACT

A local sensitivity analysis was performed for a chemically synthesized elemental sulfur (S^0)-based two-step denitrification model, accounting for nitrite (NO_2^-) accumulation, biomass growth and S^0 hydrolysis. The sensitivity analysis was aimed at verifying the model stability, understanding the model structure and individuating the model parameters to be further optimized. The mass specific area of the sulfur particles (a^*) and hydrolysis kinetic constant (k_1) were identified as the dominant parameters on the model outputs, i.e. nitrate (NO_3^-), NO_2^- and sulfate (SO_4^{2-}) concentrations, confirming that the microbially catalyzed S^0 hydrolysis is the rate-limiting step during S^0 -driven denitrification. Additionally, the maximum growth rates of the denitrifying biomass on NO_3^- and NO_2^- were detected as the most sensitive kinetic parameters.

Key words | biological surface-based hydrolysis, elemental sulfur, mathematical modeling, sensitivity analysis, two-step autotrophic denitrification

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INTRODUCTION

Globally, up to 80% of wastewater is released into the environment without adequate treatment (UN-Water 2015) affecting the water quality in ground and surface water bodies. Contamination by nitrate (NO_3^-) and nitrite (NO_2^-), due to the excessive use of N-based fertilizers and uncontrolled discharge of wastewaters, is one of the main environmental concerns (Kilic *et al.* 2014). Elevated NO_3^- concentrations result in eutrophication and ecological disturbance, while NO_2^- leads to toxicity towards aquatic life. Also, a high NO_3^- concentration imposes an adverse effect on human health such as methemoglobinemia (also known as 'blue baby' syndrome) or higher risk of cancer (Liu *et al.* 2016). Thus, the guidance value of 50 mg/l for NO_3^- was set for drinking water (WHO 2011).

NO_3^- and NO_2^- removal from wastewaters and drinking water can be performed by physico-chemical or biological processes. However, due to high costs and energy demand of the physico-chemical methods (Sierra-Alvarez *et al.*

2007), biological removal of NO_3^- (denitrification) and NO_2^- (denitritation) represents a valuable alternative technology (Mattei *et al.* 2015). Heterotrophic denitrification which uses organic compounds as energy source is a proven technology (Papirio *et al.* 2014; Zou *et al.* 2014), widely applied at the industrial scale. Notwithstanding, autotrophic denitrification has been suggested as an alternative and environmentally sustainable treatment for waters poor in carbon content, due to the costly supplementation of organics (Zhou *et al.* 2015). The use of S^0 as electron donor is easy handling and results in low operational costs and a low N_2O production (Soares 2002; Christianson *et al.* 2015). Therefore, reduced capital and operational costs, a decreased sludge production and limited greenhouse gas emissions (Kilic *et al.* 2014; Di Capua *et al.* 2015) make S^0 -based autotrophic denitrification an appropriate technology to be applied in decentralized and small-scale wastewater treatment systems.

However, chemically synthesized S^0 has a low solubility, which limits its application in autotrophic denitrification and denitrification systems. To obtain higher denitrification rates, the use of smaller and more porous S^0 particles, with a higher specific surface area, has previously been suggested (Di Capua et al. 2016). The specific surface area of the S^0 particles, thus, becomes one of the key parameters that control the autotrophic denitrification and denitrification rates (Sierra-Alvarez et al. 2007).

Modeling has proven to be an important tool for the understanding, design and control of autotrophic denitrification. Over the last years, several mathematical models accounting for S^0 -driven autotrophic denitrification have been proposed. In most of them, zero- or half-order reactions have been applied to describe the simplified S^0 -driven autotrophic denitrification kinetics without accounting for microbial growth or NO_2^- evolution (Koenig & Liu 2001; Moon et al. 2004; Qambrani et al. 2015). Xu et al. (2016) established a kinetic model for two-step autotrophic denitrification with hydrogen sulfide (H_2S) that accurately predicted the concentration of the intermediate NO_2^- . Recently, Liu et al. (2016) have developed a model for three-step autotrophic denitrification linked to H_2S and S^0 oxidation with a focus on N_2O accumulation.

However, none of the above mentioned models distinctly focused on S^0 hydrolysis as a step prior to autotrophic denitrification and denitrification (Sierra-Alvarez et al. 2007). In a recent study, a mechanistic model accounting for NO_2^- accumulation, biomass growth and S^0 hydrolysis has been proposed (Kostrytsia et al. 2018). As demonstrated through numerical simulations, the developed model could serve as a tool to predict the performance of autotrophic denitrification biofilm systems and assess their process efficiency when compared to other denitrification systems. In the present work, the model developed by Kostrytsia et al. (2018) was subjected to a sensitivity analysis to verify the model stability as well as identify the model parameters to be further optimized. Specifically, the focus was to use a local sensitivity analysis to better understand the dominant parameters of the process.

METHODS

Mathematical model overview

A mathematical model was developed by Kostrytsia et al. (2018) to dynamically simulate the main processes occurring during the two-step denitrification with S^0 (S_1). The model

takes into account the activities of a hydrolytic biomass (X_1) growing on S^0 lentils and an autotrophic denitrifying biomass (X_2) using NO_3^- (S_3) or NO_2^- (S_4) as electron acceptor and reducing them to dinitrogen gas (N_2) (S_5), and evaluates the interactions between S^0 hydrolysis and S^0 -based denitrification and denitrification. S^0 uptake was modeled by introducing a new variable, the bioavailable sulfur (S_2), which is the soluble compound directly taken up by the denitrifying bacteria for further oxidation to SO_4^{2-} (S_6). A modified surface-based kinetic equation was introduced to account for the hydrolysis of S^0 (Esposito et al. 2008). The model equations were derived from mass balances and expressed as double-Monod kinetics (Equations (1)–(8)), as reported below or in the matrix in Table 1.

$$\frac{dS_1}{dt} = -k_1 \frac{S_1}{\frac{K_1}{a^*} + S_1} X_1, \quad (1)$$

$$\begin{aligned} \frac{dS_2}{dt} = & k_1 \frac{S_1}{\frac{K_1}{a^*} + S_1} X_1 - \frac{r_1}{Y_{2,3}} \mu_{2,3}^{max} \frac{S_2}{K_{2,2} + S_2} \\ & \frac{(S_3 - S_3^*)}{K_{2,3} + (S_3 - S_3^*)} \frac{S_3}{S_3 + S_4} X_2 - \frac{r_2}{Y_{2,4}} \mu_{2,4}^{max} \\ & \frac{S_2}{K_{2,2} + S_2} \frac{(S_4 - S_4^*)}{K_{2,4} + (S_4 - S_4^*)} \frac{S_4}{S_3 + S_4} X_2, \end{aligned} \quad (2)$$

$$\frac{dS_3}{dt} = -\frac{1}{Y_{2,3}} \mu_{2,3}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_3 - S_3^*)}{K_{2,3} + (S_3 - S_3^*)} \frac{S_3}{S_3 + S_4} X_2, \quad (3)$$

$$\begin{aligned} \frac{dS_4}{dt} = & \frac{1}{Y_{2,3}} \mu_{2,3}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_3 - S_3^*)}{K_{2,3} + (S_3 - S_3^*)} \frac{S_3}{S_3 + S_4} X_2 \\ & - \frac{1}{Y_{2,4}} \mu_{2,4}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_4 - S_4^*)}{K_{2,4} + (S_4 - S_4^*)} \frac{S_4}{S_3 + S_4} X_2, \end{aligned} \quad (4)$$

$$\frac{dS_5}{dt} = \frac{1}{Y_{2,4}} \mu_{2,4}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_4 - S_4^*)}{K_{2,4} + (S_4 - S_4^*)} \frac{S_4}{S_3 + S_4} X_2, \quad (5)$$

$$\begin{aligned} \frac{dS_6}{dt} = & \frac{r_1}{Y_{2,3}} \mu_{2,3}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_3 - S_3^*)}{K_{2,3} + (S_3 - S_3^*)} \frac{S_3}{S_3 + S_4} X_2 \\ & + \frac{r_2}{Y_{2,4}} \mu_{2,4}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_4 - S_4^*)}{K_{2,4} + (S_4 - S_4^*)} \frac{S_4}{S_3 + S_4} X_2, \end{aligned} \quad (6)$$

$$\frac{dX_1}{dt} = K_0 k_1 \frac{S_1}{\frac{K_1}{a^*} + S_1} X_1 - k_{d,1} X_1, \quad (7)$$

$$\begin{aligned} \frac{dX_2}{dt} = & \mu_{2,3}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_3 - S_3^*)}{K_{2,3} + (S_3 - S_3^*)} \frac{S_3}{S_3 + S_4} X_2 \\ & + \mu_{2,4}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_4 - S_4^*)}{K_{2,4} + (S_4 - S_4^*)} \frac{S_4}{S_3 + S_4} X_2 - k_{d,2} \cdot X_2 \end{aligned} \quad (8)$$

where K_0 denotes the efficiency growth coefficient for hydrolytic biomass; r_1 and r_2 are the stoichiometric S_2 to

Table 1 | Stoichiometric matrix used for the mathematical modeling of two-step autotrophic denitrification with S^0 (adopted from Kostrytsia et al. (2018))

A_{ij}	i component →	S_1^a (mg S/l)	S_2^b (mg S/l)	S_3^c (mg N/l)	S_4^d (mg N/l)	S_5^e (mg N/l)	S_6^f (mg N/l)	X_1^g (mg VS/l)	X_2^h (mg VS/l)	Rate (mg VS/l · d)
1.	Hydrolysis of S_1	-1	1					K_0		$k_1 \frac{S_1}{\frac{K_1}{a^*} + S_1} X_1$
2.	Autotrophic growth on S_3		$-\frac{r_1}{Y_{2,3}}$	$-\frac{1}{Y_{2,3}}$	$\frac{1}{Y_{2,3}}$		$\frac{r_1}{Y_{2,3}}$		1	$\mu_{2,3}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_3 - S_3^*)}{K_{2,3} + (S_3 - S_3^*)} \frac{S_5}{S_3 + S_4} X_2$
3.	Autotrophic growth on S_4		$-\frac{r_2}{Y_{2,4}}$		$-\frac{1}{Y_{2,4}}$	$\frac{1}{Y_{2,4}}$	$\frac{r_2}{Y_{2,4}}$		1	$\mu_{2,4}^{max} \frac{S_2}{K_{2,2} + S_2} \frac{(S_4 - S_4^*)}{K_{2,4} + (S_4 - S_4^*)} \frac{S_4}{S_3 + S_4} X_2$
4.	Decay of X_1							-1		$k_{d,1} X_1$
5.	Decay of X_2								-1	$k_{d,2} X_2$

^aElemental sulfur.^bBioavailable sulfur.^cNitrate.^dNitrite.^eNitrogen gas.^fSulfate.^gHydrolytic biomass.^hDenitrifying biomass.

VS: volatile solids.

S_3 and S_2 to S_4 ratios, respectively; $Y_{2,3}$ and $Y_{2,4}$ represent the denitrifying biomass yield coefficients on NO_3^- and NO_2^- , respectively; a^* denotes the mass specific area of the sulfur particles; k_1 denotes the hydrolysis kinetic constant; K_1 indicates the volume specific half-saturation constant for S^0 ; $\mu_{2,3}^{max}$ and $\mu_{2,4}^{max}$ represent the maximum growth rates for denitrifying biomass on NO_3^- and NO_2^- , respectively; $k_{d,1}$ and $k_{d,2}$ represent the decay constants for X_1 and X_2 biomass, respectively; $K_{2,2}$, $K_{2,3}$ and $K_{2,4}$ denote the half-saturation constants for S^0 , NO_3^- and NO_2^- , respectively; S_3^* and S_4^* indicate the lowest NO_2^- and NO_3^- concentrations that enable metabolic activities of X_2 . The obtained ordinary differential equations (ODEs) were integrated by using an original software developed on the MATLAB platform and based on the numerical differentiation formulas.

The general structure of the described model is illustrated in Figure 1. Two main compartments can be individuated: the first one is related to the two-step denitrification kinetic reaction system, the second one represents the microbially catalyzed hydrolysis reaction system. The model parameters have been classified in three main groups: kinetic ($\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$, $k_{d,1}$, $k_{d,2}$, $K_{2,2}$, $K_{2,3}$, $K_{2,4}$, S_3^* and S_4^*) and stoichiometric ($Y_{2,3}$, $Y_{2,4}$, r_1 and r_2), which directly affect the two-step denitrification kinetic reaction system ('biological kinetic reaction system' in Figure 1), and hydrolysis parameters (K_0 , a^* , k_1 , K_1 and $k_{d,1}$) which are related to the S^0 hydrolysis compartment. K_0 represents the efficiency

growth coefficient for X_1 ; r_1 and r_2 are the stoichiometric S_2 to S_3 and S_2 to S_4 ratios, respectively. The values of $Y_{2,3}$, $Y_{2,4}$, $K_{2,2}$, $K_{2,4}$, r_1 , r_2 , $k_{d,1}$ and $k_{d,2}$ were adopted from previous studies (Sierra-Alvarez et al. 2007; Sin et al. 2008; Liu et al. 2016; Xu et al. 2016) (Table 2). The optimal values of $\mu_{2,3}^{max}$ and $\mu_{2,4}^{max}$ were deducted from both the denitrification and denitrification experiments (Table 2).

Sensitivity analysis

The model proposed by Kostrytsia et al. (2018) requires a high dimensional (stoichiometric, kinetic and hydrolysis-related) parameter space to be explored. To estimate each parameter, excess experimental results should be provided to avoid ill-conditioning of the parameter estimation (Kesavan & Law 2005). Therefore, a model sensitivity analysis was performed to identify the parameter targets for further experimental exploration (Jarrett et al. 2015). The low-sensitive parameters have a negligible effect on the predictions, whereas the highly sensitive parameters require some level of certainty to make robust model predictions (Croicu et al. 2017).

In this model, a local sensitivity analysis was performed to compute sensitivity functions for the dynamic simulations with the initial conditions of 30 mg/l NO_2^- -N and 210 mg/l NO_3^- -N, originating from the kinetic experiments (Kostrytsia et al. 2018). The stoichiometric ratios (r_1 and r_2) were

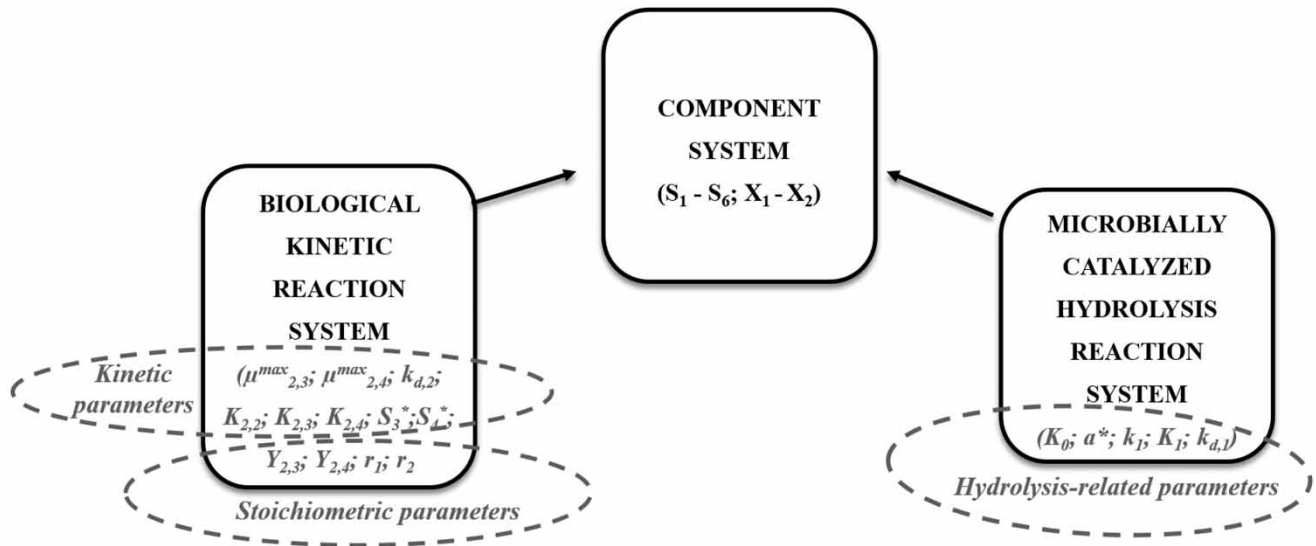


Figure 1 | General model structure describing the microbially catalyzed S^0 hydrolysis and two-step autotrophic denitrification kinetics. The model parameters influencing each reaction system are mentioned in italics.

Table 2 | Stoichiometric and kinetic parameters (with nominal values) of the developed model for two-step autotrophic denitrification with S^0 (adopted from Kostrytsia et al. (2018))

Parameter		Value	Unit	Source
Stoichiometric parameters				
$Y_{2,3}$	Yield coefficient for X_2 on S_3	0.25	mg VS/mg N	Xu et al. (2016)
$Y_{2,4}$	Yield coefficient for X_2 on S_4	0.28	mg VS/mg N	Xu et al. (2016)
r_1	S_2 to S_3 stoichiometric ratio	1.2	mg S/mg N	Sierra-Alvarez et al. (2007)
r_2	S_2 to S_4 stoichiometric ratio	0.55	mg S/mg N	Sierra-Alvarez et al. (2007)
Kinetic parameters				
K_0	Efficiency growth coefficient for X_1	0.1	mg VS/mg S	Kostrytsia et al. (2018)
$\mu_{2,3}^{max}$	Maximum growth rate for X_2 on S_3	0.0067	1/d	Kostrytsia et al. (2018)
$\mu_{2,4}^{max}$	Maximum growth rate for X_2 on S_4	0.0058	1/d	Kostrytsia et al. (2018)
$K_{2,2}$	Half-saturation constant for S_2	0.215	mg S/l	Liu et al. (2016)
$K_{2,3}$	Half-saturation constant for S_3	36	mg N/l	Kostrytsia et al. (2018)
S_3^*	The threshold value for S_3	35	mg N/l	Kostrytsia et al. (2018)
$K_{2,4}$	Half-saturation constant for S_4	40	mg N/l	Xu et al. (2016)
S_4^*	The threshold value for S_4	37	mg N/l	Kostrytsia et al. (2018)
K_1	Volume specific half-saturation constant for S_1	5.1	1/dm	Kostrytsia et al. (2018)
k_1	Hydrolysis kinetic constant	0.12	mg S/mg VS d	Kostrytsia et al. (2018)
a^*	Mass specific area	0.0008164	dm ² /mg	Kostrytsia et al. (2018)
$k_{d,1}$	Decay rate coefficient for X_1	0.0006	1/d	Sin et al. (2008)
$k_{d,2}$	Decay rate coefficient for X_2	0.0006	1/d	Sin et al. (2008)

VS: volatile solids.

calculated on the biotransformation mechanism and obtained by previous experimental studies (Sierra-Alvarez et al. 2007). Thus, r_1 and r_2 were not re-estimated in the current study. Additionally, the influence of the biomass decay

rates ($k_{d,1}$ and $k_{d,2}$) of the microorganisms performing S^0 -driven denitrification and denitritation was out of investigation, as $k_{d,1}$ and $k_{d,2}$ were very low (Liu et al. 2016). Also, the threshold values for NO_3^- and NO_2^- (S_3^* and S_4^* ,

respectively), which represent the concentration values below which the microorganisms are not able to grow, were not considered for the sensitivity analysis. Therefore, the sensitivity analysis was conducted for the following 11 parameters: $\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$, $K_{2,2}$, $K_{2,3}$ and $K_{2,4}$ (kinetic), $Y_{2,3}$ and $Y_{2,4}$ (stoichiometric) and K_0 , a^* , k_1 and K_1 (hydrolysis-related). NO_3^- -N, NO_2^- -N and SO_4^{2-} -S concentrations were set as the focused variables to measure the sensitivity.

The sensitivities were calculated as the effect of the change in the input parameters on the model output over a time span of 22 days. An automatic differentiation tool SENS_SYS coupled with the ODE solver of MATLAB was used to predict the local sensitivity. The SENS_SYS tool is an extension of the ODE15s tool that allows the solving of the ODE system while computing derivatives (sensitivities) of the solution with respect to parameters (Molla & Padilla 2002). The accuracy of the SENS_SYS tool is controlled by the default relative tolerance of 1×10^{-6} . The sensitivity analysis of the system F was calculated by differentiating the system with respect to the kinetic parameter u , as illustrated in Equation (9).

$$F(t, y, y', u) = 0 \quad (9)$$

where t denotes the time interval for the integration (days), y represents the input state variable, y' the first derivative of y with respect to t , and u denotes the parameter.

RESULTS AND DISCUSSION

Parameter sensitivity overview on NO_3^- -N, NO_2^- -N and SO_4^{2-} -S concentrations

The absolute sensitivities of the 11 parameters (K_0 , $Y_{2,3}$, $Y_{2,4}$, a^* , k_1 , K_1 , $\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$, $K_{2,2}$, $K_{2,3}$ and $K_{2,4}$) to the input state variables (i.e. 210, 0 and 0 mg/L of NO_3^- -N, NO_2^- -N and SO_4^{2-} -S, respectively) are shown in Figure 2. The nominal values of the parameters used for the model (Equations (1)–(8)) are listed in Table 2.

The $Y_{2,3}$, $Y_{2,4}$, a^* , k_1 , $\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$ and $K_{2,2}$ parameters were sensitive to some extent to at least one of the model outputs, i.e. NO_3^- -N, NO_2^- -N and SO_4^{2-} -S (Figure 2). Both NO_3^- -N and NO_2^- -N process variables were highly sensitive to a^* , $\mu_{2,3}^{max}$ and $\mu_{2,4}^{max}$. It is noteworthy to highlight that a negative value of the absolute sensitivity refers to the reduction of the process variables with parameter perturbation. For example, the

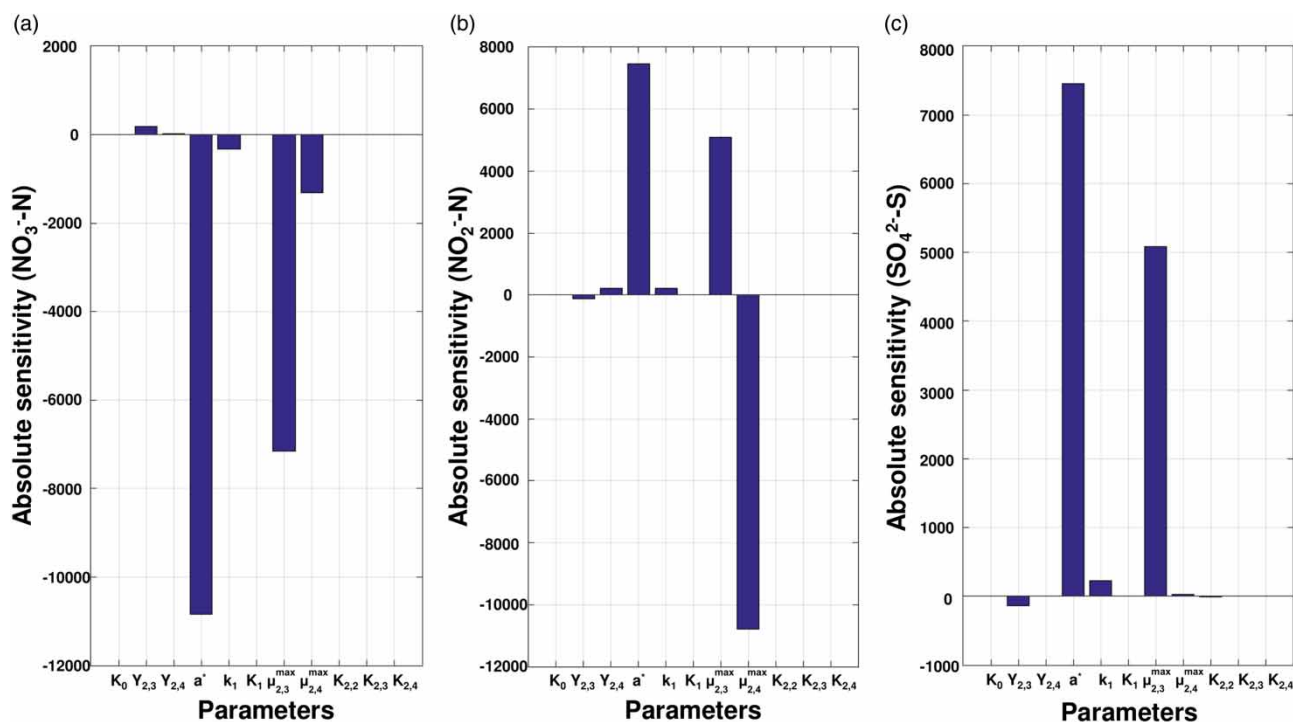


Figure 2 | Absolute (or local) sensitivities of kinetic parameters during the simulation time for the degradation of (a) NO_3^- -N and (b) NO_2^- -N and the production of (c) SO_4^{2-} -S.

negative value of $\mu_{2,3}^{max}$ sensitivity for NO_3^- -N indicated NO_3^- -N consumption (Figure 2(a)), while the positive value of $\mu_{2,3}^{max}$ sensitivity for NO_2^- -N corresponded to NO_2^- -N production (Figure 3(a)). The NO_3^- and NO_2^- reduction was coupled to S^0 biooxidation in order to produce energy and facilitate microbial growth. Therefore, the use of NO_3^- or NO_2^- as a substrate for the microbial cultures resulted in a high sensitivity of the $\mu_{2,3}^{max}$ and $\mu_{2,3}^{max}$ to the model outputs (Figure 2).

The sensitivity analysis results suggest that the parameter vector can be reduced to a^* , k_1 , $\mu_{2,3}^{max}$ and $\mu_{2,4}^{max}$, based on the minimum magnitude of significance considered (200 as absolute sensitivity). The parameters deemed not to be sufficiently significant can be fixed at their nominal values (Table 2). Further investigation might be related to such a reduced model both in terms of assumed parameter distribution and experimental calibration. Further calibration is required for the most sensitive model parameters to improve the quality of the model. However, the values of absolute sensitivity for K_0 , K_1 , $K_{2,3}$ and $K_{2,4}$ for each process variable were significantly lower than those of $Y_{2,3}$, $Y_{2,4}$, a^* , k_1 , $\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$ and $K_{2,2}$. The effect of each sensitive parameter on the process variables should be investigated in more detail due to their crucial role in the model calibration.

Sensitivity analysis for kinetic ($\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$, $K_{2,2}$, $K_{2,3}$ and $K_{2,4}$) and stoichiometric ($Y_{2,3}$ and $Y_{2,4}$) model parameters

To investigate the effect of each parameter on the process variables, a series of sensitivity curves was obtained by

changing the five kinetic ($\mu_{2,3}^{max}$, $\mu_{2,4}^{max}$, $K_{2,2}$, $K_{2,3}$ and $K_{2,4}$), and the two stoichiometric ($Y_{2,3}$ and $Y_{2,4}$) parameters one by one during the simulation. The effect of each parameter on the input state variables NO_3^- -N, NO_2^- -N and SO_4^{2-} -S is illustrated in Figure 3. The greater parameter line slope indicates the more significant role of the parameter in the autotrophic denitrification process.

The most sensitive kinetic parameters were the maximum growth rate of the denitrifying biomass on NO_3^- ($\mu_{2,3}^{max}$) and NO_2^- ($\mu_{2,4}^{max}$) as illustrated in Figures 2(a)–2(c) and 3(d)–3(e), with a more significant effect on NO_3^- -N from day 10 to day 15 when the denitrification rate was higher (Kostrytsia et al. 2018). The SO_4^{2-} -S absolute sensitivity was 10,000 and 7,500 for $\mu_{2,3}^{max}$ and $\mu_{2,4}^{max}$ (Figure 2), respectively. This was likely attributed to the higher metabolic rates, in particular S^0 oxidation to SO_4^{2-} , of the denitrifying bacteria growing on NO_3^- ($\mu_{2,3}^{max}$) rather than on NO_2^- . On the other hand, the half-saturation constants for S_2 ($K_{2,2}$), S_3 ($K_{2,3}$) and S_4 ($K_{2,4}$) had a minimal impact on the model outputs (Figure 3(c), 3(f) and 3(g)). A larger set of experimental data would be required to get an accurate evaluation of the half-saturation constants. More data could be obtained from kinetic tests with different initial substrate concentrations for a reliable model calibration of the half-saturation constants.

Regarding the stoichiometric parameters, the denitrifying biomass yield coefficient on NO_3^- ($Y_{2,3}$) showed a high sensitivity for NO_3^- -N, NO_2^- -N and SO_4^{2-} -S outputs (Figure 3(a)). The highest sensitivity of the $Y_{2,3}$ was observed between days 10 and 15 due to the higher denitrification rate.

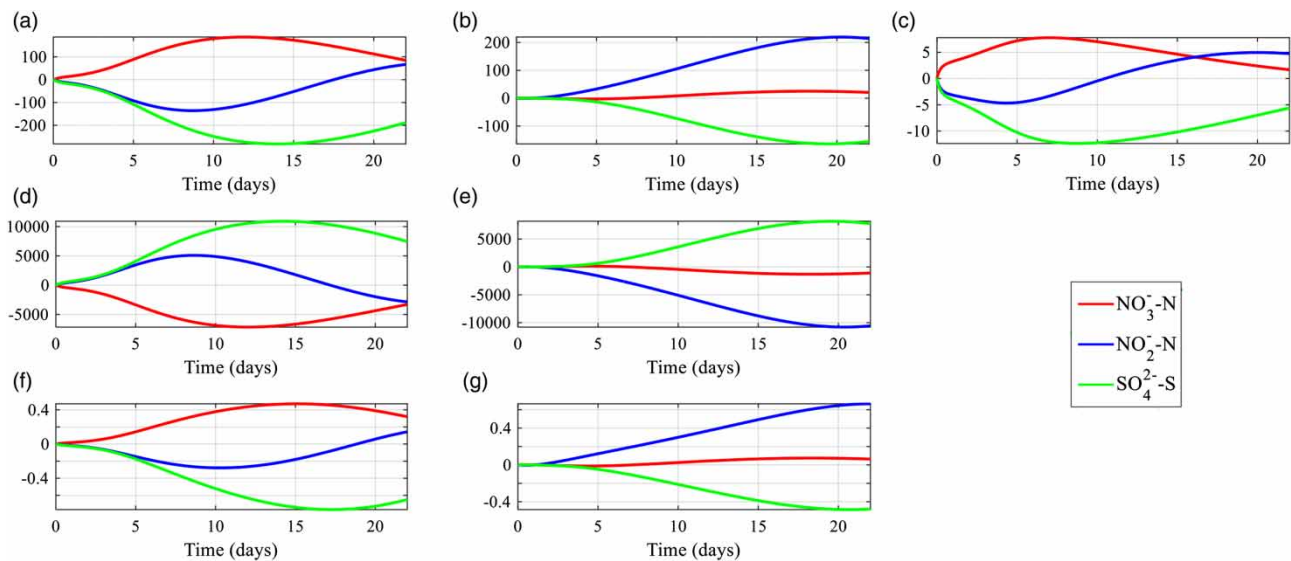


Figure 3 | Output absolute (or local) sensitivity of kinetic and stoichiometric parameters: (a) $Y_{2,3}$, (b) $Y_{2,4}$, (c) $K_{2,2}$, (d) $\mu_{2,3}^{max}$, (e) $\mu_{2,4}^{max}$, (f) $K_{2,3}$ and (g) $K_{2,4}$.

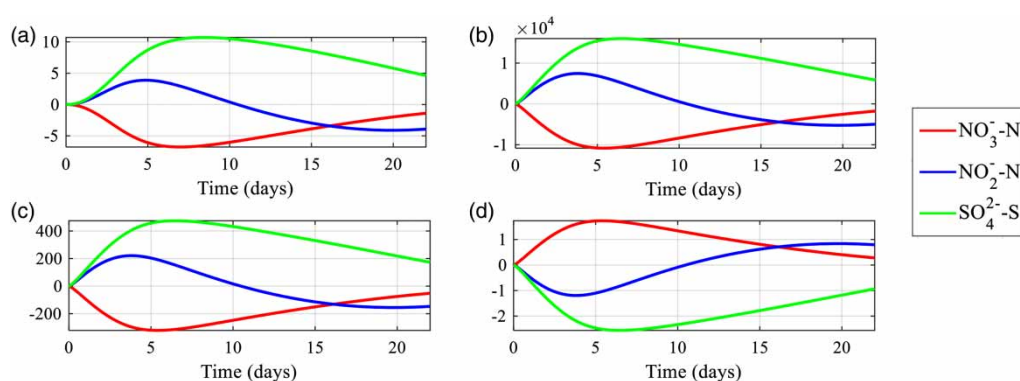


Figure 4 | Output absolute (or local) sensitivity of hydrolysis-related parameters: (a) K_0 , (b) a^* , (c) k_1 and (d) K_1 .

The effect of $Y_{2,4}$ sensitivity on the NO_2^- -N and SO_4^{2-} -S outputs increased with time due to the accumulation of NO_2^- -N as an intermediate product of the NO_3^- -N degradation.

Sensitivity analysis for hydrolysis-related (K_0 , a^* , k_1 and K_1) model parameters

The effect of hydrolysis-related model parameters (K_0 , a^* , k_1 and K_1) on the input state variables NO_3^- -N, NO_2^- -N and SO_4^{2-} -S is illustrated in Figure 4. The mass specific area of the sulfur particles (a^*) posed, apparently, a major influence on the model outputs and was ranked as a first dominant parameter (Figure 2). The parameter a^* accounts for the overall surface area of the sulfur particles to be microbially solubilized prior to denitrification and denitritation. As illustrated in Figure 4(b), the NO_3^- -N output was more sensitive to the change in parameter a^* , compared to NO_2^- -N. The latter might be attributed to the higher stoichiometric S/N ratio required for complete denitrification than for denitritation. This is consistent with the literature, where the impact of the specific surface area of sulfur particles was suggested as a prerequisite of S^0 oxidation coupled to denitrification (Wang et al. 2016). The model proposed by Kostrytsia et al. (2018) describes the surface-based S^0 hydrolysis as an inevitable aspect and rate-limiting step in the denitrification and denitritation processes, and the high sensitivity of parameter a^* to the model outputs confirmed the significance of the used hydrolysis approach.

Among the other parameters related to the S^0 hydrolysis step, the hydrolysis kinetic constant (k_1), being dependent on the nature of sulfur, possessed a high sensitivity for the model output variables (Figure 4(c)). The absolute sensitivity of both parameters a^* and k_1 showed a peak between days 5 and 10 due to the high denitrification rate, and then slowly dropped (Figure 4(b) and 4(c), respectively). Consequently,

the model predictions and calibration are crucial during that phase. On the other hand, the efficiency growth coefficient for hydrolytic biomass (K_0) and volume specific half-saturation constant for S^0 (K_1) did not significantly influence the model outputs (Figure 4(a) and 4(d), respectively).

CONCLUSIONS

In this work, the results of a local sensitivity analysis performed on a newly developed model for microbially-catalyzed elemental S^0 hydrolysis and two-step denitrification were presented. The sensitivity analysis provided a few insights on the importance of parameter values and their impact on process dynamics. The sensitivity analysis demonstrated that the model was more sensitive to the mass specific area of the sulfur particles (a^*), hydrolysis kinetic constant (k_1) and the maximum growth rate of the denitrifying biomass on NO_3^- ($\mu_{2,3}^{max}$) and NO_2^- ($\mu_{2,4}^{max}$). The high sensitivity of hydrolysis-related parameters (a^* and k_1) to the input state variables (NO_3^- -N, NO_2^- -N and SO_4^{2-} -S) confirmed the importance of including the microbially catalyzed surface-based S^0 hydrolysis as a limiting process step in the two-step denitrification model. Further experimental and modeling investigations should thus focus on the S^0 hydrolysis.

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NOTES

The authors have no competing interests to declare.

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